

Experimental Implementation of a Nonlinear Control Method for Magnetostrictive Transducers

William S. Oates, Phillip Evans, Ralph C. Smith and Marcelo J. Dapino

Abstract—In this paper, we discuss the development and experimental implementation of a nonlinear control design for magnetostrictive transducers operating in hysteretic regimes. The hysteresis and constitutive nonlinearities are characterized using a homogenized energy framework based on energy relations at the lattice level employed in combination with stochastic homogenization techniques that incorporate material and field nonhomogeneities. Using this framework, we employ nonlinear optimal control theory to construct open loop inputs for tracking. We subsequently employ PI-based perturbation feedback to ensure robustness with respect to model uncertainty and sensor noise. Experimental implementation results at frequencies up to 1000 Hz demonstrate the feasibility of the method for high speed tracking while operating in highly nonlinear operating regimes.

I. INTRODUCTION

Present and emerging automotive, industrial, aeronautic, aerospace and biomedical applications require actuators that provide large force, high accuracy, moderate stroke, broadband capabilities. Moreover, the actuators often must be compact, reconfigurable and multifunctional. For a number of applications, transducers employing ferroelectric or ferromagnetic drive elements meet these criteria and are being considered for high performance control systems. Two common ferroelectric and ferromagnetic actuator materials are lead zirconate titanate (PZT) and Terfenol-D.

Whereas these compounds provide unique actuator capabilities, they also exhibit hysteresis and constitutive nonlinearities that must be accommodated in models, transducer designs, and model-based control designs to achieve stringent tracking and control specifications. The fact that the hysteresis and nonlinearities are rate, stress, and temperature-dependent compound the challenge of high performance actuator design.

The most obvious way to limit hysteresis and nonlinear effects is to restrict devices to low or moderate drive regimes. Whereas this is feasible for some applications, it excludes the devices from many high performance applications where can prove advantageous over traditional actuators. Secondly,

feedback can be used to linearize the material behavior for certain operating regimes. However, it is illustrated in [9] and Section IV that the authority of feedback algorithms degrades at high frequencies. PZT-based devices can also be linearized to a certain degree through the use of current or charge-controlled amplifiers [6], [7]. However, this can prove expensive when compared with more traditional voltage-controlled amplifiers, and current-control is ineffective for maintaining a fixed dc bias as required for various applications — e.g., maintaining a fixed position with an x -stage while sweeping with a y -stage in an atomic force microscope.

In this paper, we experimentally demonstrate the feasibility of a nonlinear control design for high speed, high accuracy tracking. For brevity, we focus on a magnetic device but the models and model-based control design are equally applicable to ferroelectric materials — e.g., PZT-based devices. The tracking application is motivated by recent investigations focused on the use of Terfenol-D transducers to mill automotive components at high speed while maintaining micron-level tolerances; however, the problem and general formulation are ubiquitous for a wide range of applications.

There are essentially two strategies to control hysteretic actuators using nonlinear models. The first is to use the characterization framework to construct an approximate nonlinear inverse that linearizes the actuator response in the manner depicted in Figure 1(a) — e.g., see [24]. Linear control algorithms are then used to achieve control objectives. This method has the advantage of linear control designs but has the disadvantage that the model inverse may be difficult to

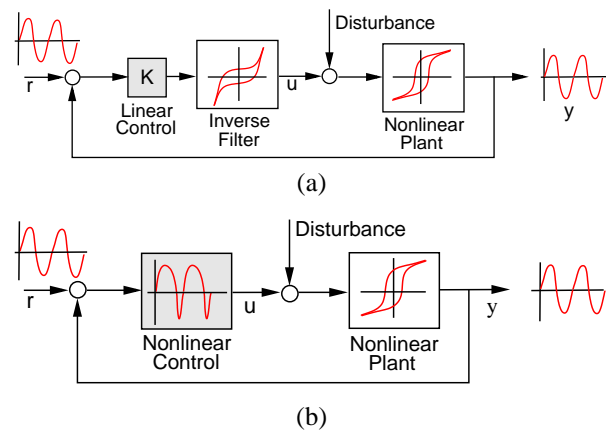


Fig. 1. (a) Linear control design employing a nonlinear, model-based inversed compensator, and (b) nonlinear model-based control design.

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initiate and implement at high speed. Moreover, scaling or mapping may be required to convert amplifier outputs (e.g., voltage, current, or field) to inverse inputs (e.g., magnetization). Within the context of ferroelectric and ferromagnetic actuators, this approach has been employed using Preisach models, domain wall models and homogenized energy models. We note that experimental implementation of open-loop and feedback designs employing Preisach-based inverse compensators are reported in [3], [8], [21]–[23] whereas open loop experimental control implementation of a homogenized energy inverse are reported in [4].

The second strategy is to construct nonlinear control designs which yield input signals that directly incorporate actuator nonlinearities as depicted in Figure 1(b) — e.g., see [13], [25]. If optimal control theory is employed, this approach requires the approximate solution of a two-point boundary value problem which can be computationally intensive. However, this technique avoids the real-time implementation of the model inverse and scaling issues associated with inverse compensators.

In this paper, we demonstrate the experimental implementation of a nonlinear control based on the homogenized energy framework for characterizing hysteresis in ferromagnetic materials. Open loop control inputs are computed offline through the approximation of a two-point boundary value problem derived using optimal control theory. To provide robustness with regard to model and measurement errors, one can either linearize about the optimal state and control to construct a linear perturbation model that is amenable to LQR design, or employ direct PI feedback on measured perturbations about the optimal state. We employ the latter technique since implementation in this manner provides the efficiency of classical PI designs while accommodating frequency-dependent hysteresis and nonlinear material dynamics via the nonlinear open-loop signal.

The hysteresis characterization framework and transducer model are summarized in Section II. The nonlinear open loop and perturbation designs are discussed in Section III, and the experimental performance of the technique at frequencies up to 1000 Hz is illustrated in Section IV.

II. NONLINEAR CONSTITUTIVE RELATIONS AND TRANSDUCER MODEL

We summarize here the ferromagnetic hysteresis framework developed in [16], [20] and use it to construct a model that characterizes the dynamics of the experimental magnetic transducer. As detailed in [14], [19], analogous relations quantify the hysteresis inherent to PZT and hence the framework is applicable to a range of ferroic compounds. It is noted in [4], [14], [18] that whereas the homogenized energy framework provides an energy basis for certain extended Preisach models, it fundamentally differs from classical Preisach models in a number of aspects including the direct incorporation of thermal relaxation mechanisms and the capability that it provides to characterize noncongruent behavior.

A. Constitutive Relations

Letting H and M denote the magnetic field and magnetization, we consider the lattice-level Gibbs energy relation

$$G(H, M) = \psi(M) - HM \quad (1)$$

where the Helmholtz energy is given by

$$\psi(M) = \begin{cases} \frac{1}{2}\eta(M + M_R)^2 & , M \leq -M_I \\ \frac{1}{2}\eta(M - M_R)^2 & , M \geq M_I \\ \frac{1}{2}\eta(M_I - M_R) \left(\frac{M^2}{M_I} - M_R \right) & , |M| < M_I. \end{cases} \quad (2)$$

Here M_I, M_R and η respectively denote the positive inflection point, the local remanent magnetization, and the reciprocal slope after switching.

As detailed in [14], [16], [20], the balance of G and the relative thermal energy kT/V , where k, T and V respectively denote Boltzmann's constant, temperature in degrees Kelvin, and a reference volume, yields the kernel relation

$$\overline{M}(H) = x_+ \langle M_+ \rangle + x_- \langle M_- \rangle \quad (3)$$

which characterizes hysteresis at the lattice level. The fractions x_+ and x_- of positively and negatively oriented dipoles are quantified by the differential equations

$$\begin{aligned} \dot{x}_+ &= -p_{+-}x_+ + p_{-+}x_- \\ \dot{x}_- &= -p_{-+}x_- + p_{+-}x_+ \end{aligned} \quad (4)$$

and the expected magnetizations due to positively and negatively oriented moments are

$$\begin{aligned} \langle M_+ \rangle &= \frac{\int_{M_I}^{\infty} M e^{-G(H, M)V/kT} dM}{\int_{M_I}^{\infty} e^{-G(H, M)V/kT} dM}, \\ \langle M_- \rangle &= \frac{\int_{-\infty}^{-M_I} M e^{-G(H, M)V/kT} dM}{\int_{-\infty}^{-M_I} e^{-G(H, M)V/kT} dM}. \end{aligned} \quad (5)$$

The likelihoods of switching from positive to negative, and conversely, are given by

$$\begin{aligned} p_{+-} &= \frac{1}{\mathcal{T}(T)} \frac{\int_{M_I-\epsilon}^{M_I} e^{-G(H, M)V/kT} dM}{\int_{M_I-\epsilon}^{\infty} e^{-G(H, M)V/kT} dM}, \\ p_{-+} &= \frac{1}{\mathcal{T}(T)} \frac{\int_{-M_I}^{-M_I+\epsilon} e^{-G(H, M)V/kT} dM}{\int_{-\infty}^{-M_I+\epsilon} e^{-G(H, M)V/kT} dM} \end{aligned} \quad (6)$$

where ϵ is taken to be a small positive constant. The relaxation time \mathcal{T} is the reciprocal of the frequency at which dipoles attempt to switch — see [14], [16], [20] for details.

To incorporate the effects of polycrystallinity, material nonhomogeneities, and variable interaction fields, we assume that local coercive and interaction fields are manifestations of distributions having associated densities $\nu_1(H_c)$ and $\nu_2(H_I)$. This yields the macroscopic field-magnetization relation

$$M(H) = \int_{-\infty}^{\infty} \int_0^{\infty} \overline{M}(H + H_I; H_c) \nu_1(H_c) \nu_2(H_I) dH_c dH_I. \quad (7)$$

For the device characterization results summarized in Section IV, values for the discretized densities were estimated using the techniques detailed in [14], [17].

B. Transducer Model

To model the experimental transducer depicted in Figure 2, we assume that the Terfenol-D rod has area A , length ℓ , Young's modulus Y , density ρ , and Kelvin-Voigt damping parameter C . The longitudinal displacement of the rod tip is denoted by u_ℓ .

It is shown in [14] that the uniaxial stress σ is related to the magnetization, given by (7), via the constitutive relation

$$\sigma = Y\varepsilon + C\dot{\varepsilon} - a_1(M - M_0) - a_2(M - M_0)^2 \quad (8)$$

where Y is the elastic modulus at constant magnetization, ε is the longitudinal strain, C is the Kelvin-Voigt damping parameter, a_1 is the piezomagnetic coefficient, and a_2 is the magnetostrictive coefficient. The bias magnetization M_0 includes the effects of a permanent magnet and the initial magnetized state of the material.

We make the assumption that strains are uniform and given by

$$\varepsilon(t) = \frac{u_\ell(t)}{\ell}. \quad (9)$$

Balancing the forces σA for the rod with those of the restoring mechanism yields the lumped model

$$\begin{aligned} \rho A \ell \frac{d^2 u_\ell}{dt^2}(t) + \frac{CA}{\ell} \frac{du_\ell}{dt}(t) + \frac{YA}{\ell} u_\ell(t) \\ = -m_\ell \frac{d^2 u_\ell}{dt^2}(t) - c_\ell \frac{du_\ell}{dt}(t) - k u_\ell(t) \\ + A a_1 [M(H(t)) - M_0] + A a_2 [M(H(t)) - M_0]^2 \end{aligned}$$

or, equivalently,

$$\begin{aligned} m \frac{d^2 u_\ell}{dt^2}(t) + c \frac{du_\ell}{dt}(t) + k u_\ell(t) \\ = \tilde{a}_1 [M(H(t)) - M_0] + \tilde{a}_2 [M(H(t)) - M_0]^2 \end{aligned} \quad (10)$$

where

$$\begin{aligned} m = \rho A \ell + m_\ell, \quad c = \frac{CA}{\ell} + c_\ell, \quad k = \frac{YA}{\ell} + k_\ell \\ \tilde{a}_1 = A a_1, \quad \tilde{a}_2 = A a_2. \end{aligned} \quad (11)$$

The initial conditions are $u_\ell(0) = u_0$ and $\frac{du_\ell}{dt}(0) = u_1$. The magnetization M is specified by the model (7).

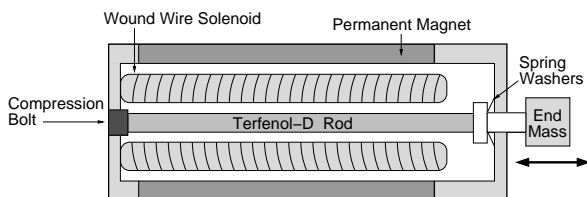


Fig. 2. Magnetic transducer design employed in the control experiments.

The model can subsequently be written as the first-order system

$$\begin{aligned} \dot{x}(t) &= Ax(t) + B(H(t)) \\ x(0) &= x_0 \end{aligned} \quad (12)$$

where $x(t) = [u_\ell(t), \dot{u}_\ell(t)]^T$, $x_0 = [u_0, u_1]^T$ and

$$\begin{aligned} A &= \begin{bmatrix} 0 & 1 \\ -k/m & -c/m \end{bmatrix} \\ B(H) &= [\tilde{a}_1(M(H) - M_0) + \tilde{a}_2(M(H) - M_0)^2] \begin{bmatrix} 0 \\ 1/m \end{bmatrix}. \end{aligned}$$

In the subsequent control formulation, the input is taken to be $u = H$ or $u = nI$ where I denotes the current applied to the solenoid and n is the number of coils per unit length.

III. PERTURBATION CONTROL FORMULATION

A. Open Loop Control

We summarize here the open loop optimal control formulation detailed in [10], [12]. We let r denote a reference signal to be tracked, $y(t) = Cx(t)$ denote observations and let $e(t) = Cx(t) - r(t)$ designate the error. The augmented penalty functional is taken to be

$$\begin{aligned} \bar{J} &= \frac{1}{2} [Cx(t_f) - r(t_f)]^T P [Cx(t_f) - r(t_f)] \\ &+ \int_{t_0}^{t_f} [\mathcal{H} - \lambda^T(t) \dot{x}(t)] dt \end{aligned} \quad (13)$$

where λ denotes the adjoint variable, the Hamiltonian is

$$\begin{aligned} \mathcal{H} &= \frac{1}{2} [e(t)^T Q e(t) + u^T(t) R u(t)] \\ &+ \lambda^T [Ax(t) + B(u)(t)], \end{aligned} \quad (14)$$

and Q, R respectively penalize large errors and control inputs.

Enforcement of necessary conditions to minimize (13) — see [2], [5] — yields the control input relation

$$u^*(t) = -R^{-1} \left(\frac{\partial B(u)}{\partial u} \right)^T \lambda(t) \quad (15)$$

along with the two-point boundary value problem

$$\dot{z}(t) = F(t, z) \quad (16)$$

where $z = [x, \lambda]^T$ and

$$F(t, z) = \begin{bmatrix} Ax(t) + B(u)(t) \\ -A^T \lambda(t) - C^T Q C x(t) + C^T Q r(t) \end{bmatrix}. \quad (17)$$

To approximate the solution to (16), we employ a finite difference discretization defined on the grid $t_j = j\Delta t$, where $\Delta t = \frac{t_f}{N}$ and $j = 0, \dots, N$. Letting $z_j \approx z(t_j)$, this yields the discrete system

$$\begin{aligned} \frac{1}{\Delta t} [z_{j+1} - z_j] &= \frac{1}{2} [F(t_j, z_j) + F(t_{j+1}, z_{j+1})] \\ E_0 z_0 &= [x_0, 0]^T \\ E_f z_N &= [0, -C^T P r(t_f)]^T. \end{aligned} \quad (18)$$

The solution of (18) can be expressed as the problem of finding $z_h = [z_0, \dots, z_N]$ which solves

$$\mathcal{F}(z_h) = 0. \quad (19)$$

A quasi-Newton iteration of the form

$$z_h^{k+1} = z_h^k + \xi_h^k, \quad (20)$$

where ξ_h^k solves

$$\mathcal{F}'(z_h^k) \xi_h^k = -\mathcal{F}(z_h^k), \quad (21)$$

is then used to approximate the solution to (19). The Jacobian has the form

$$\mathcal{F}'(z_h) = \begin{bmatrix} S_0 & R_0 & & & \\ & S_1 & R_1 & & \\ & & \ddots & \ddots & \\ & & & S_{N-1} & R_{N-1} \\ E_0 & & & & E_f \end{bmatrix} \quad (22)$$

where

$$S_i = -\frac{1}{\Delta t} \begin{bmatrix} I & 0 \\ 0 & I \end{bmatrix} - \frac{1}{2} \begin{bmatrix} A & \frac{\partial}{\partial \lambda} B[u_i^*] \\ -C^T Q C & -A^T \end{bmatrix}. \quad (23)$$

The representation for R_i is similar.

Remark 3.1: It is shown in [13] that an analytic LU decomposition can be determined for $\mathcal{F}(z_h^k)$. This significantly reduces memory requirements and is fundamental for efficient solution since it reduces the dimension of the linear system solution to 8. For the results reported in Section IV, solution of (19), and hence computation of a nonlinear control input, took on the order of 7 seconds.

B. Perturbation Feedback

The relation (15) provides an open loop control signal that is optimal for given Q, R in the absence of model or measurement error. To provide robustness with regard to such uncertainties, we consider perturbation feedback as detailed in [2], [5]. Linearization about the optimality system yields

$$\begin{aligned} \delta \dot{x}(t) &= A \delta x(t) + B \delta u(t) \\ \delta y(t) &= C \delta x(t) \\ \delta x(0) &= \hat{x}_0 \end{aligned} \quad (24)$$

where $\delta u, \delta x$ and δy are first-order variations about u^*, x^* and y^* .

To facilitate experimental implementation, we use classical PI control to compute δu ; that is, we take

$$\delta u(t) = -K_P e(t) - K_I \int_0^t e(s) ds. \quad (25)$$

The final control input is then

$$u(t) = u^*(t) + \delta u(t). \quad (26)$$

Remark 3.2: The computation of the open loop input u^* is performed off-line and hence does not affect implementation speed. The computation of δu can be performed at the same speed as classical PI implementation. Hence the experimental implementation of the perturbation control is as efficient as standard PI implementation.

IV. EXPERIMENTAL RESULTS

The control algorithm was implemented on a magnetostrictive transducer having a Terfenol-D rod of length 0.1 m and diameter of 0.0125 m. The preload on the rod was 10-14 MPa and it was subjected to a magnetic field bias of approximately 40 kA/m. Strains at the end of the rod were measured with a capacitive sensor having a sensitivity of 2.5 mV and a bandwidth of 12.5 kHz.

To ensure that the transducer was initialized to the maximal remanent value prior to characterization and control experiments, each data set was initiated by a half-cycle of a 1 Hz sine wave having an amplitude of 1 volt (this corresponds to a current of 4.6 amp). Sinusoidal input voltages and corresponding output displacements were subsequently collected at 100, 200, 300 and 500 Hz. As illustrated in Figure 3, the degree of hysteresis exhibited by the device is highly frequency-dependent thus necessitating the incorporation of magnetic moment dynamics via the relations (3) and (4), and the rod dynamics modeled by (10). Details regarding the characterization of the nonlinear voltage-current relation are provided in [9].

To construct the model, the parameters $M_r, \eta, \tau, \gamma, a_1, a_2, m, c, k$ and densities ν_1 and ν_2 were estimated through a least squares fit to the combined set of 100, 200, 300 and 500 Hz data. The resulting model fit is plotted in Figure 4. The model with this parameter set was then employed in all control experiments.

To illustrate the tracking capability of the nonlinear control design, experiments were performed at 100, 200, 300, 500, 700 and 1000 Hz. The amplitude of a sinusoidal reference signal was chosen to be 300 ppm which represents an operating regime in which hysteresis and constitutive nonlinearities are significant — see Figure 3.

The open loop and perturbation feedback control results at 200 Hz are respectively plotted in Figures 5 and 6 whereas analogous results at 1000 Hz are plotted in Figures 7 and 8. For both frequencies, it is noted that whereas the open loop control (15) provides reasonable accuracy, the inclusion of the perturbation feedback term (26) improves the accuracy

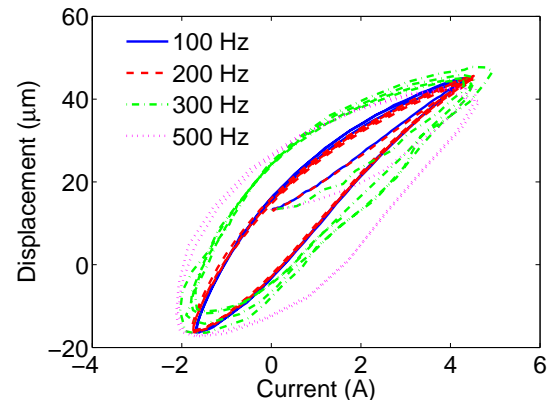
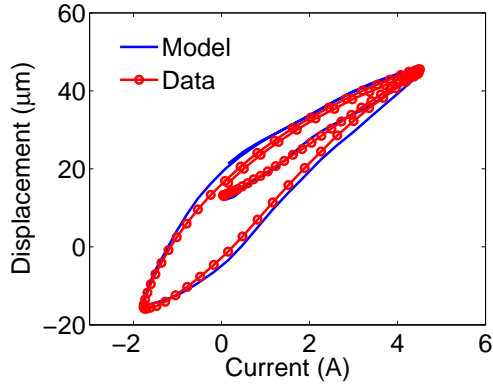
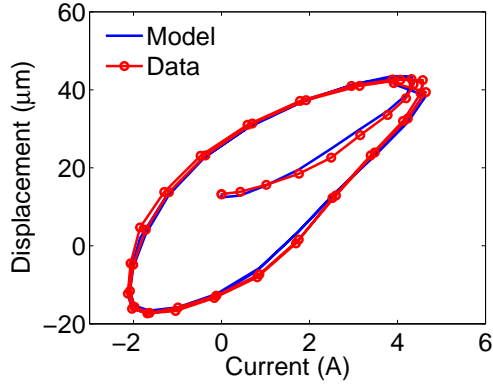


Fig. 3. Frequency-dependent current-strain data at 100, 200, 300 and 500 Hz.



(a)



(b)

Fig. 4. Model fit to the experimental data at (a) 200 and (b) 500 Hz.

of both the magnitude and phase. We point out that the characterization experiments did not include 1000 Hz data; hence the accuracy of the nonlinear model-based control at this frequency illustrates the predictive capability of the model.

To provide an initial comparison between the nonlinear control technique discussed here and classical PI designs, the tracking authority achieved with PI inputs at 1000 Hz is illustrated in Figure 9. At this frequency, neither the correct amplitude nor phase are achieved thus yielding errors on the order of the reference signal. It is detailed in [9],

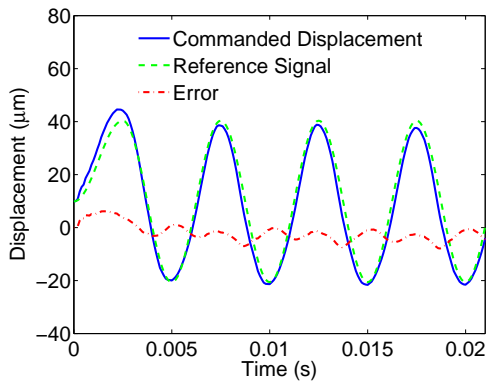


Fig. 5. Nonlinear open loop tracking authority provided by (15) at 200 Hz.

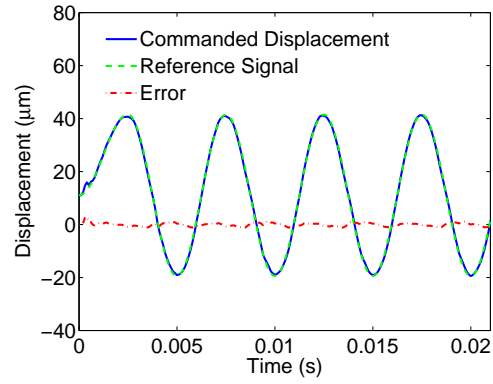


Fig. 6. Tracking authority provided by the perturbation feedback control (26) at 200 Hz.

where a complete comparison between the two designs at multiple frequencies are reported, that with the 10 kHz sample frequency, PI control is viable at frequencies below approximately 500 Hz. At higher frequencies, the nonlinear control framework proves advantageous since it provides high accuracy while retaining the implementational efficiency of classical PI designs.

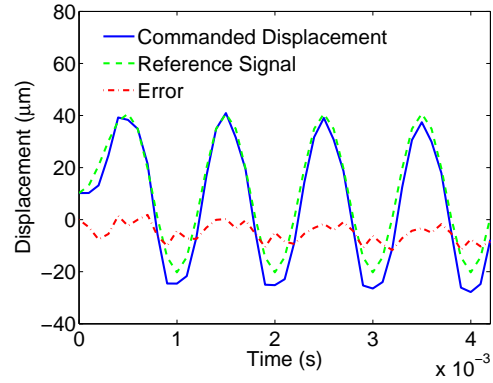


Fig. 7. Nonlinear open loop tracking authority provided by (15) at 1000 Hz.

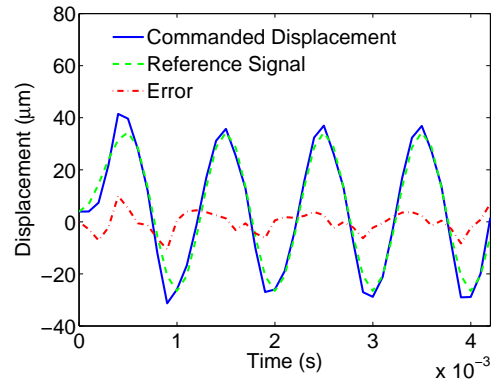


Fig. 8. Tracking authority provided by the perturbation feedback control (26) at 1000 Hz.

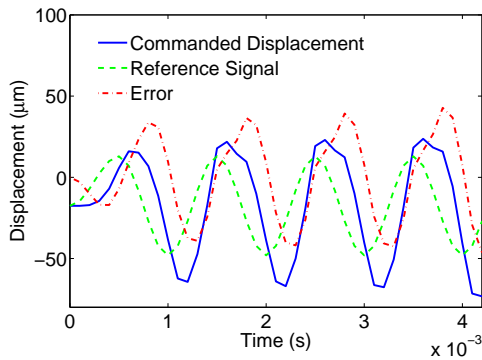


Fig. 9. Tracking authority provided by PI control at 1000 Hz.

V. CONCLUDING REMARKS

In this paper, we report initial experimental results demonstrating the tracking authority provided by a nonlinear control design for magnetostrictive transducers operating in highly nonlinear and hysteretic regimes. The control design is comprised of a nonlinear open loop component, based on a homogenized energy model, employed in combination with a perturbation PI feedback component. Because the open loop gains are computed off-line, the closed loop implementation provides the efficiency of classical PI control but with significantly enhanced tracking capability at high frequencies since the model-based open loop control incorporates frequency-dependent hysteresis and constitutive nonlinearities. This significantly extends the results of [10], [12] which focused solely on the numerical implementation of the control design.

The present experimental results illustrate sinusoidal tracking at frequencies up to 1 kHz for a magnetic actuator. However, the unified nature of the characterization framework [14], [19] permits direct extension of the theory to ferroelectric (e.g., PZT) and ferroelastic (e.g., SMA) devices. The numerical implementation of an analogous control design for PZT stages is illustrated in [11] for a variety of reference signals and the experimental implementation of PZT control design is under present investigation.

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